Year 12 Extension 1

2.

Applications of Calculus to the Physical World (2U) Assignment Date Due:

- 1. A cubical block of ice has an edge of 10 cm. It melts so that its volume decreases at a constant rate of 25 cm³ per hour and the block remains cubical. Find:
 - (a) the volume V at any time t.
 - (b) the time required to completely melt the ice.
 - The mass M of a radioactive substance is initially 10 grams and 20 years later its mass it 9.6 grams.
 - (a) Find the annual decay rate given that the rate of decay of a radioactive substance is proportional to the mass of that substance present at any time (ie $\frac{dM}{dt} = -kM$)
 - (b) In how many years will the mass be halved?
- 3. A radio-active material decays according to the exponential function $M = M_0 e^{kt}$. If the initial mass is 50 grams and the mass after 10 years is 40 grams, find:
 - (a) the value of k
 - (b) the amount of material present after 15 years.
 - (c) the half-life of the material. (The half-life of a radio-active material is the time taken for the material to halve its mass)
- 4. A particle starts from rest 5 m from a fixed point O and moves in a straight line with an acceleration a = 3t 4. Find the velocity and position of the particle and at time *t*.
- 5. A particle is moving in a straight line in such a way that its distance, x metres, from a fixed point O, in the line, after t seconds is given by $x = 4t 5t^2 + 2t^3$. Find:
 - (a) the difference in position from when t = 2 and t = 3.
 - (b) the velocity after 2 seconds.
 - (c) the time when the particle is at rest.
 - (d) where the particle is at rest.
 - (e) the maximum velocity reached by the particle.
- 6. The position x m at any time t seconds of a particle moving in a straight line is given by $x = 2t^3 9t^2 + 12t + 6$. Find:
 - (a) when its acceleration is zero and its velocity at that time.
 - (b) when its velocity is zero and its acceleration at that time.
- 7. A particle moves in a straight line and at any time *t* seconds, its velocity *v* m/s is given by $v = e^{-t}$. If initially the particle is 2 m from a fixed point O in the line, find its position *x* at any time *t*. Sketch the graph of *x* as a function of *t*.
- 8. A particle moves in a straight line so that at any time t its velocity is given by $v = \frac{1}{1+t}$.
 - (a) If its distance from a fixed point O in the line is x, show that $x = \log_e(1 + t)$ given that x = 0 when t = 0.
 - (b) Show that the particle is moving away from O as t increases.
 - (c) Find the acceleration when t = 0.