

For questions 1 – 20, differentiate each function with respect to x .

1. $y = (x + 6)(x^2 + 3)$

2. $y = 2x^2(x^2 - 5)$

3. $y = (3x + 4)^4$

4. $y = \sqrt{2x + 8}$

5. $y = \frac{1}{x+1}$

6. $y = \frac{2x+1}{2x-1}$

7. $y = \frac{x^2}{1-x^2}$

8. $y = \frac{1}{(2x+3)^5}$

9. $y = x^{\frac{2}{3}}$

10. $y = (x^2 + 1)(x^2 - 6)$

11. $y = \sqrt{4x - 1}$

12. $y = \frac{x}{x+1}$

13. $y = (3 - 2x)^4$

14. $y = \frac{1}{(2 - 3x)^4}$

15. $y = (x+1)\sqrt{x}$

16. $y = x^3(1+x)^3$

17. $y = \frac{5x-2}{3x+5}$

18. $y = \frac{x^3-1}{x+1}$

19. $y = \frac{x}{\sqrt{x^2+1}}$

20. $y = (x+1)^2(x+2)^3$

21. Find the equation of the tangent to the curve $y = \frac{2}{x+1}$ at the point where $x = 3$.

22. Find the slope of the curve $y = \frac{2}{x^2+1}$ at the origin. Find the equation of the tangent and the normal at the origin.

23. Find the point where the curve $y = (2x - 5)^3$ cuts the x -axis and find the slope of the tangent at this point.

24. Find the equation of the tangent to the curve $y = \frac{x^2}{4-x}$ at the point $(2, 2)$

25. Differentiate each of the following functions with respect to x .

(a) $f(x) = \frac{x}{\sqrt{x}}$

(b) $f(x) = (2x + 1)^2(5x - 4)^3$

(c) $f(x) = \frac{4x}{\sqrt{2x}}$

26. Find the equations of the tangent and normal to the curve $y = x^{\frac{3}{2}}$ at the point $(4, 8)$.

If the tangent meets the x -axis at T and the normal meets the x -axis at N, show that $TN = 26^{\frac{2}{3}}$