

Parameters

- **The parabola $x^2 = 4ay$**
Can be written as $x = 2at$ and $y = at^2$ where t is the parameter
- **The Chord**
Joining the points $P(2ap, ap^2)$ and $Q(2aq, aq^2)$ on the parabola $x^2 = 4ay$ has:
 - gradient $= \frac{p+q}{2}$
 - equation $y - \frac{1}{2}(p+q)x + apq = 0$
 - $pq = -1$ if it is a focal chord
 - parameters of the endpoints are $p, \frac{-1}{p}$ if it is a focal chord
- **Parametric Differentiation**
Given that $y = f(t)$ and $x = f(t)$ then:
$$\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx}$$
- **Equation of tangent and normal to the parabola**
 - equation of tangent at (x_1, y_1) is: $xx_1 = 2ay + 2ay_1$
 - equation of the tangent at t : $y - tx + at^2 = 0$
 - equation of the normal at (x_1, y_1) is: $y - y_1 = \frac{-2a}{x_1}(x - x_1)$
 - equation of the normal at ' t ' is: $x + ty = at^3 + 2at$
 - gradient of the tangent at the point where $x = t$ is: t
 - gradient of the normal at the point where $x = t$ is: $-\frac{1}{t}$
- **Further points on the parabola $x^2 = 4ay$ [$P(2ap, ap^2)$ and $Q(2aq, aq^2)$]**
 - **Chord PQ;**
 - gradient $= \frac{p+q}{2}$
 - equation is $y - \frac{1}{2}(p+q)x + apq = 0$
 - **Tangent at P;**
 - gradient $= p$
 - equation is $y - px + ap^2 = 0$
 - tangents at P and Q meet at $[a(p+q), apq]$
 - equation of the tangent at (x_1, y_1) is: $x_1x = 2a(y + y_1)$
 - **Normal at P;**
 - gradient $= \frac{-1}{p}$
 - equation is $x + py = ap^3 + 2ap$
 - normals at P and Q meet at $[-apq(p+q), a(p^2 + pq^2 + q^2 + 2)]$
 - equation of the normal at (x_1, y_1) is: $x_1x = y - y_1 = \frac{-2a}{x_1}(x - x_1)$
 - **Focal chord;**
 - endpoints have parameters p and $\frac{-1}{p}$
 - tangents at endpoints intersect at right angles on the directrix
- **Equation of the chord of contact**
 $x_1x = 2a(y + y_1)$